

Temple Geometry

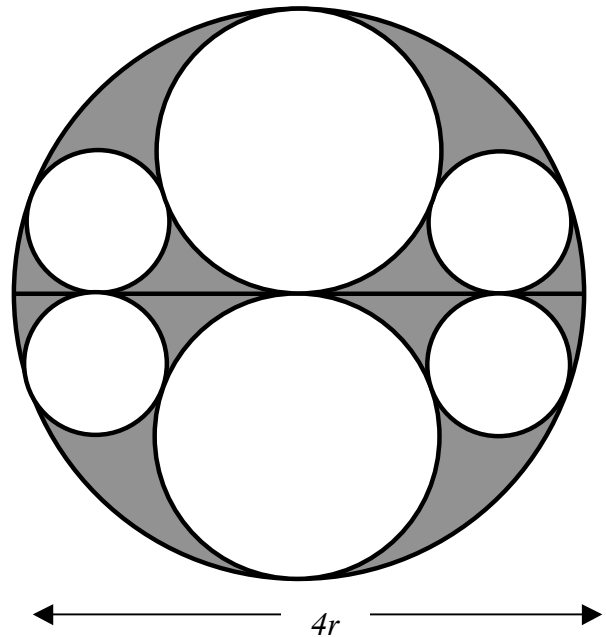
During the Edo period (1603-1867) of Japanese history, geometrical puzzles were hung in the holy temples as offerings to the gods and as challenges to worshippers.

This is one such problem.

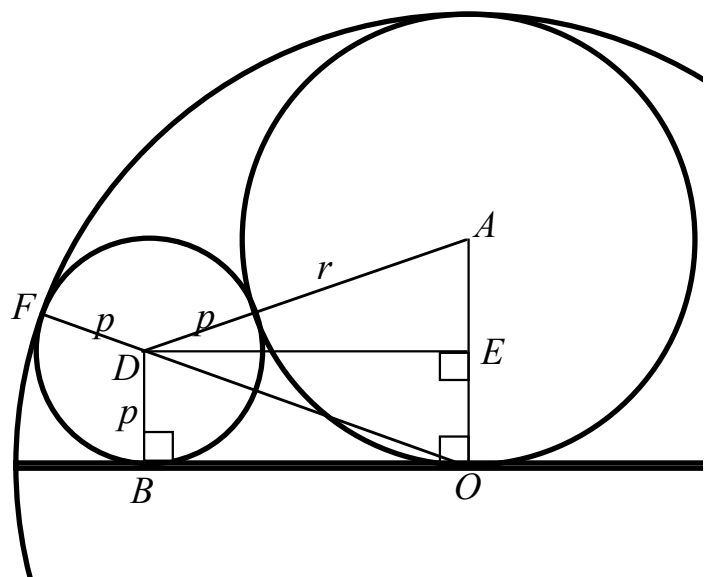
Inside a large circle with radius $2r$, two circles of radius r are drawn.

Four smaller circles, of radius p , are drawn to touch the large circle and the circles of radius r .

The following questions will help you to find the relationship between r and p



1. In the right triangle DOB , explain why the length of OD is $2r - p$



2. Use the Pythagorean theorem in triangle DOB to find an expression for OB^2 .

3. In the right triangle ADE, explain why the length of AE is $r - p$.

4. Use the Pythagorean theorem in triangle ADE to find an expression for ED^2 .

5. Use your results from questions 2 and 4, and the fact that $OB = ED$ to show that $r = 2p$

6. Show that the shaded area of the diagram has area πr^2 .

Temple Geometry		Rubric	
		Points	Section points
1.	OF = radius of large circle = 2r. FD = p, so OD is 2r - p	2	2
2.	$OB^2 = DO^2 - DB^2$ $= (2r - p)^2 - p^2$ $= 4r^2 - 4pr$ <i>Partial credit for some correct work</i>	2 (1)	2
3.	AO = r and EO = p, so AE is r - p	1	1
4.	$ED^2 = DA^2 - AE^2$ $= (r + p)^2 - (r - p)^2$ $= 4pr$ <i>Partial credit for some correct work</i>	2 (1)	2
5.	Since $OB^2 = ED^2$, $4r^2 - 4pr = 4pr$ $\therefore 4r^2 = 8pr$ $\therefore r = 2p$	2	2
6.	Shows that the Shaded area = $4\pi r^2 - 2\pi r^2 - 4\pi(r/2)^2 = \pi r^2$	1	1
Total Points			10